



Improving performance of cascade refrigeration system using low GWP refrigerants for some cities in Russia

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April 2021

Introduction

Modeling

Validation

Optimization

Results

Conclusion

Source of Heat pump

Air

Waste water

Ground

- Not useful in cold climate condition
- Low cost of installation
- Not need to drill
- Capable to use in residential and commercial buildings

- Useful in cold climate condition
- High cost of installation
- Need to drill
- Capable to use in residential and commercial buildings

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Optimization
of performance

Max COP

Max exergy
efficiency

Min total
cost

Parameters

Evaporator and condenser temperature, power consumption, Cooling or heating capacity, climate conditions, soil thermal properties, soil depth,

List of the studies about optimization of heat pumps

References	Refrigerant	Heat source	Optimization
Jin et al. [13]	CO ₂	Ground	Energy
Sarbu et al. [14]	CFC	Ground	Energy, economic and environmental
Sivasakthive et al. [15]	R22	Ground	Energy
Onder Ozgener et al. [16]	R22	Ground-solar	Energy, Exergy efficiency
H. Weeratunge et al [17]	Water	Ground-solar	Energy, economic

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Innovation

Using cascade
refrigeration
system

Exergy-
economic
analysis

Investigation
5 cities in
Russia

1- COP
2- Exergy efficiency
3- Total cost rate

1- Climate condition
2- Soil thermal properties
3- Soil temperature

1- Optimal value of evaporator temperature
2- Optimal value of condensation cascade temperature
3- Selection the best value of COP, exergy and cost

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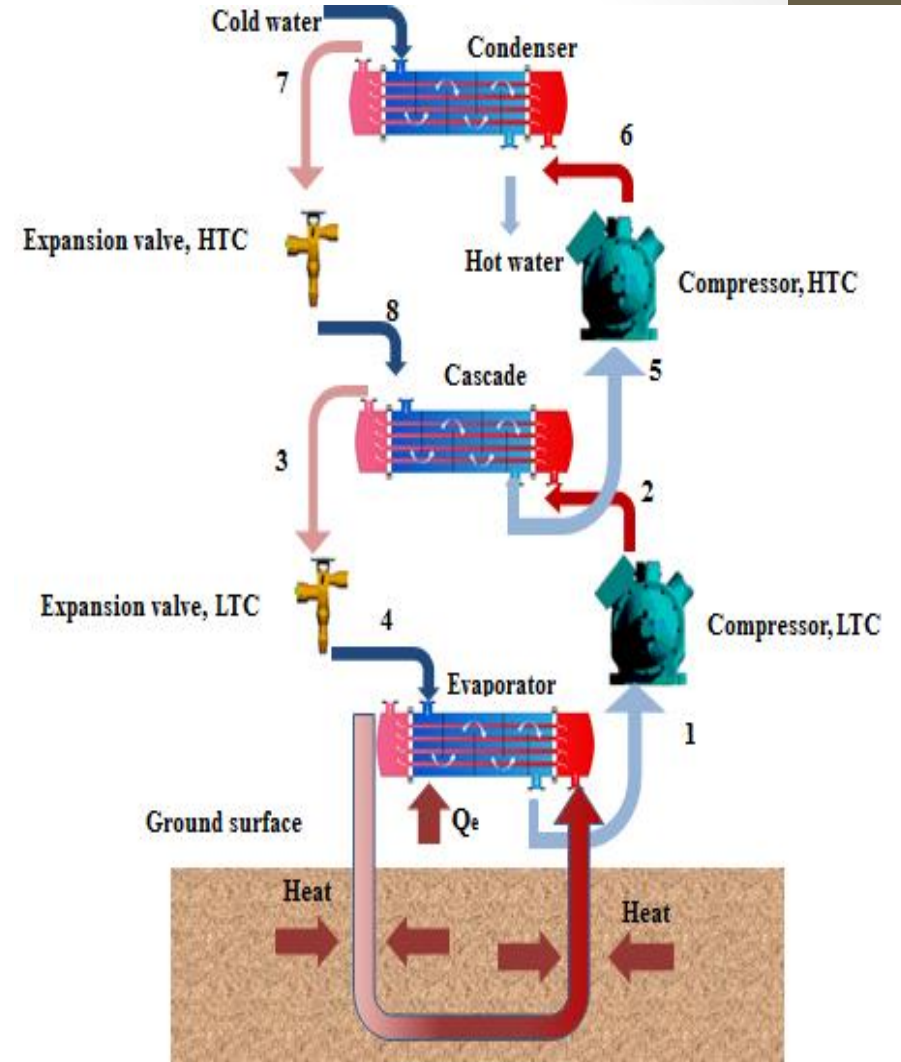
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- Refrigerant receives heat from ground at point 4 and leaves evaporator in the form of saturated vapor.
- Saturated vapor becomes superheated at point 2 through a compression process that is assumed adiabatic.
- Heat is transferred from high pressure refrigerant in LTC to HTC refrigerant.
- In 5-6 process, refrigerant becomes superheated by means of HTC compressor.
- The high pressure and temperature refrigerant in condenser rejects heat to the water for domestic application and then HTC refrigerant is converted to the saturated liquid state at condenser outlet (point 7).



Cycle	Refrigerant	Critical temperature (°C)	Boiling point (°C)	ODP	GWP
HTC	R161	102.2	-37.1	0	12
LTC	R41	44.1	-78.1	0	97

Geographical region

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City	Average winter temperature (°C)	Humidity (%)
Yekaterinburg	-17	80
Nizhny Novgorod	-15	83
Moscow	-13	82
Saint Petersburg	-10	83
Sochi	5	75

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Energy-exergy analysis

Evaporator:

$$\dot{m}_4 = \dot{m}_1 = \dot{m}_{LTC}$$

$$\dot{Q}_{eva} = \dot{m}_{LTC}(h_4 - h_1)$$

$$\dot{E}x_{eva} = \dot{m}_{LTC}(ex_4 - ex_1) + \dot{Q}_{eva}\left(1 - \frac{T_{air}}{T_{eva}}\right)$$

LTC and HTC Compressor:

$$\dot{m}_2 = \dot{m}_1 = \dot{m}_{LTC}, \dot{m}_5 = \dot{m}_6 = \dot{m}_{HTC}$$

$$\dot{W}_{com,LTC} = \dot{m}_{LTC}(h_2 - h_1), \dot{W}_{com,HTC} = \dot{m}_{HTC}(h_6 - h_5)$$

$$\dot{E}x_{com,LTC} = \dot{m}_{LTC}(ex_1 - ex_2) + \dot{W}_{com,LTC}, \dot{E}x_{com,HTC} = \dot{m}_{HTC}(ex_5 - ex_6) + \dot{W}_{com,HTC}$$

$$\dot{W}_{tot} = \dot{W}_{com,HTC} + \dot{W}_{com,LTC}$$

$$\eta_{com,LTC} = \frac{h_{2s} - h_1}{h_2 - h_1}, \eta_{com,HTC} = \frac{h_{6s} - h_5}{h_6 - h_5}$$

Condenser:

$$\dot{m}_6 = \dot{m}_7 = \dot{m}_{HTC}$$

$$\dot{Q}_{con} = \dot{m}_{HTC}(h_6 - h_7)$$

$$\dot{E}x_{con} = \dot{m}_{HTC}(ex_6 - ex_7) + \dot{Q}_{con}\left(1 - \frac{T_{air}}{T_{con}}\right)$$

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LTC and HTC Expansion Valve:

$$\dot{m}_7 = \dot{m}_8 = \dot{m}_{HTC}, \dot{m}_3 = \dot{m}_4 = \dot{m}_{LTC}$$

$$h_7 = h_8, h_3 = h_4$$

$$\dot{E}x_{exp,HTC} = \dot{m}_{LTC}(ex_7 - ex_8), \dot{E}x_{exp,LTC} = \dot{m}_{LTC}(ex_3 - ex_4)$$

Cascade Heat Exchanger:

$$\dot{m}_2 + \dot{m}_8 = \dot{m}_3 + \dot{m}_5$$

$$\dot{Q}_{cas} = \dot{m}_{LTC}(h_3 - h_2)$$

$$\dot{E}x_{cas} = \dot{m}_{LTC}(ex_2 - ex_3) + \dot{m}_{HTC}(ex_8 - ex_5)$$

$$COP = \frac{\dot{Q}_{eva}}{\dot{W}_{tot}}$$

$$\dot{e}x = \dot{m}[(h - h_{air}) - T_{air}(s - s_{air})]$$

Total exergy destruction

$$\dot{E}x_{tot} = \dot{E}x_{eva} + \dot{E}x_{con} + \dot{E}x_{com,HTC} + \dot{E}x_{com,LTC} + \dot{E}x_{cas} + \dot{E}x_{exp,HTC} + \dot{E}x_{exp,LTC}$$

$$\eta_{ex} = \frac{\dot{W}_{tot} - \dot{E}x_{tot}}{\dot{W}_{tot}}$$

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Economic-environmental analysis

Total cost rate

Cost rate due to CO₂ emission

$$\dot{Z}_{tot} = \sum \dot{Z}_{cm} + \dot{Z}_{op} + \dot{Z}_{em}$$

Capital and maintenance cost

Operational cost

Operational hours

Electricity price

Emission factor

CO₂ penalty price

$$\dot{Z}_{op} = Nh \times \dot{W}_{tot} \times \beta_{el}$$

$$\dot{Z}_{em} = \mu_{CO_2} \times \dot{W}_{tot} \times \beta_{CO_2}$$

Installation cost of 61 \$ per meter depth from the ground surface is added to the total cost of GSHP system.

$$CRF = \frac{ir(ir + 1)^n}{(1 + ir)^n - 1}$$

Interest rate of $ir=14\%$
and life time of $n=15$
year

$$\phi=1.06$$

Component	Capital and maintenance cost rate
Evaporator	$\phi \times CRF \times 1397 \times A_{eva}^{0.89}$
Compressor, LTC	$\phi \times CRF \times 10167.5 \times \dot{W}_{com,LTC}^{0.46}$
Compressor, HTC	$\phi \times CRF \times 9624.2 \times \dot{W}_{com,HTC}^{0.46}$
Condenser	$\phi \times CRF \times 383.5 \times A_{con}^{0.65}$
Expansion Valve, HTC	$\phi \times CRF \times 114.5 \times \dot{m}_{HTC}$
Expansion Valve, LTC	$\phi \times CRF \times 114.5 \times \dot{m}_{LTC}$
Cascade heat exchanger	$\phi \times CRF \times 383.5 \times A_{cas}^{0.65}$

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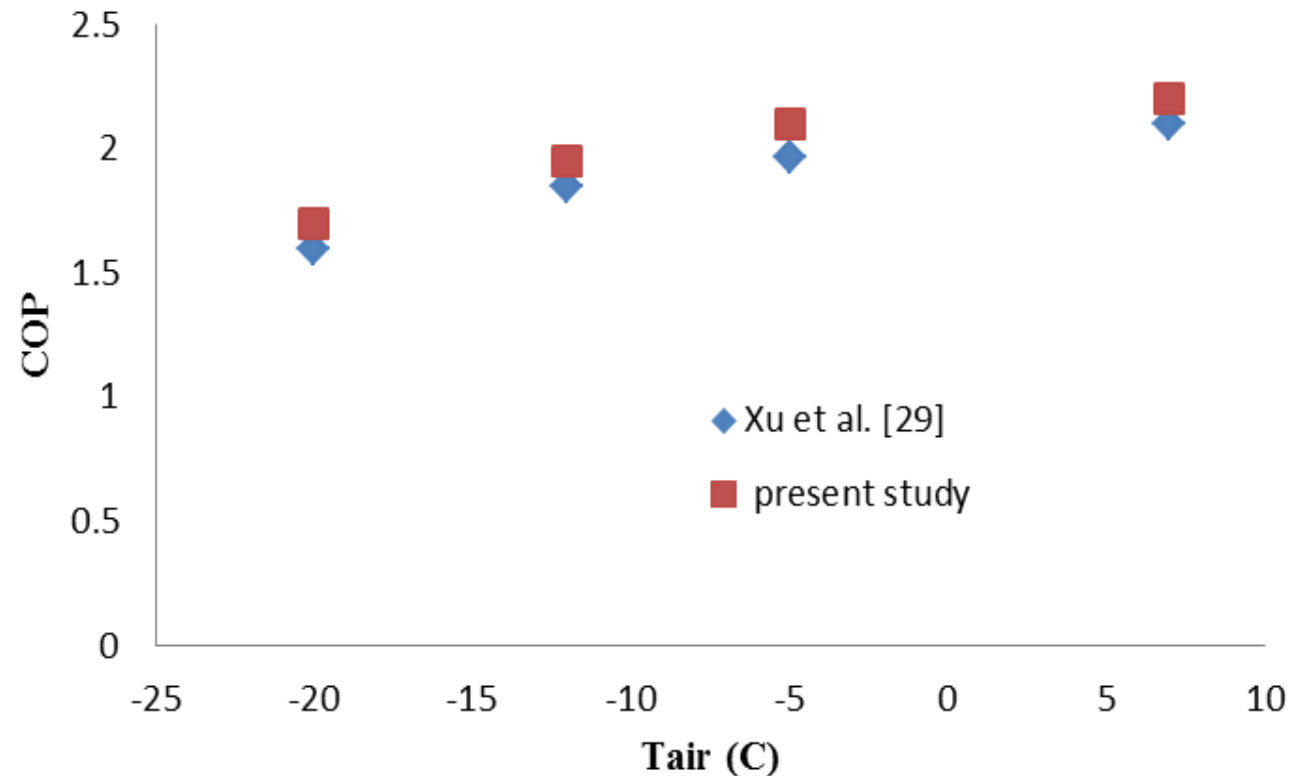
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- Cascade air source heat pump
- Increasing temperature of water as high as 75 °C using R404A and R134a in LTC and HTC
- COP variations in terms of ambient temperature



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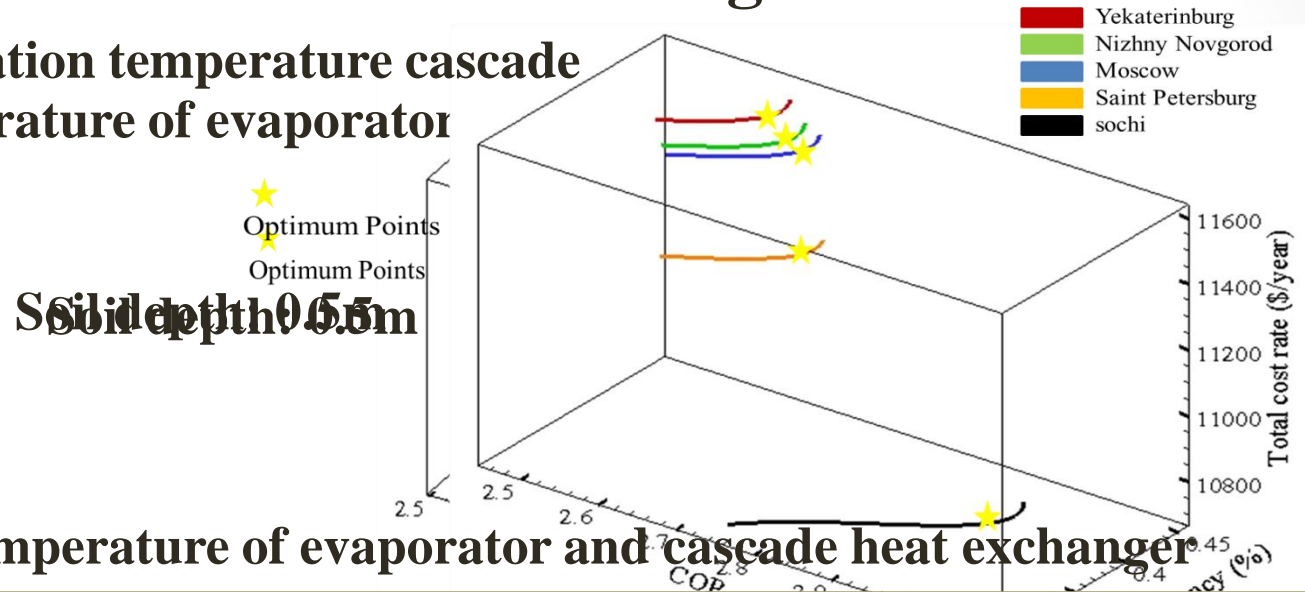
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Optimal temperature of evaporator and condensation cascade heat exchanger

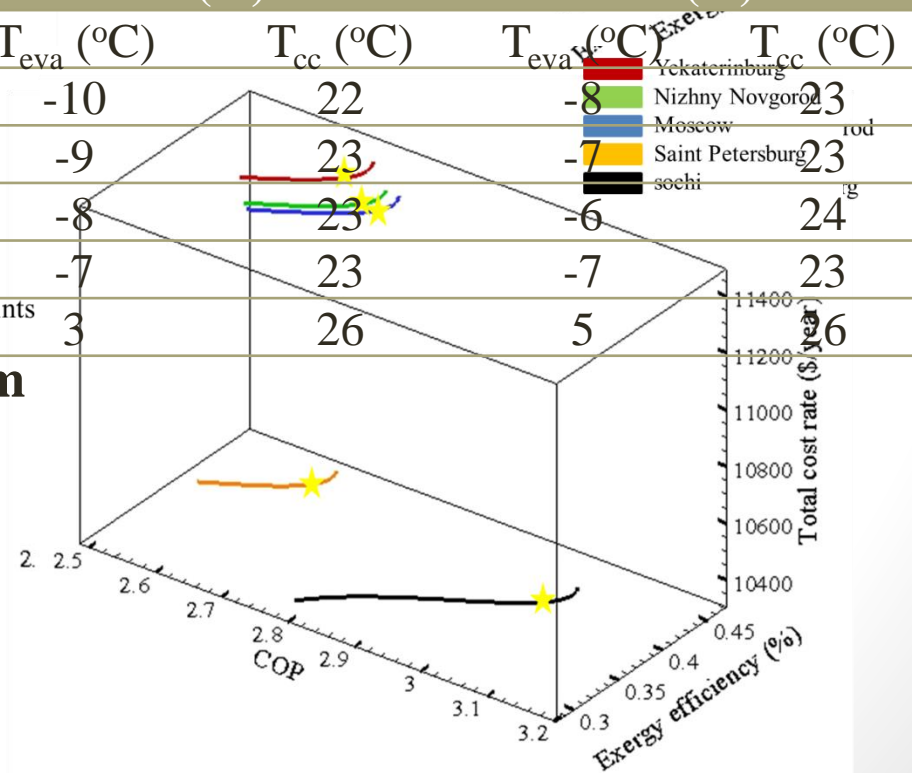
Optimal condensation temperature cascade Optimal temperature of evaporator



Optimal temperature of evaporator and cascade heat exchanger

City	0.5 (m)		1 (m)	
	T_{eva} (°C)	T_{cc} (°C)	T_{eva} (°C)	T_{cc} (°C)
1 Yekaterinburg	-10	22	-8	23
2 Nizhny Novgorod	-9	23	-7	23
3 Moscow	-8	23	-6	24
4 Saint Petersburg	-7	23	-7	23
5 Sochi	3	26	5	26

Soil depth: 1m



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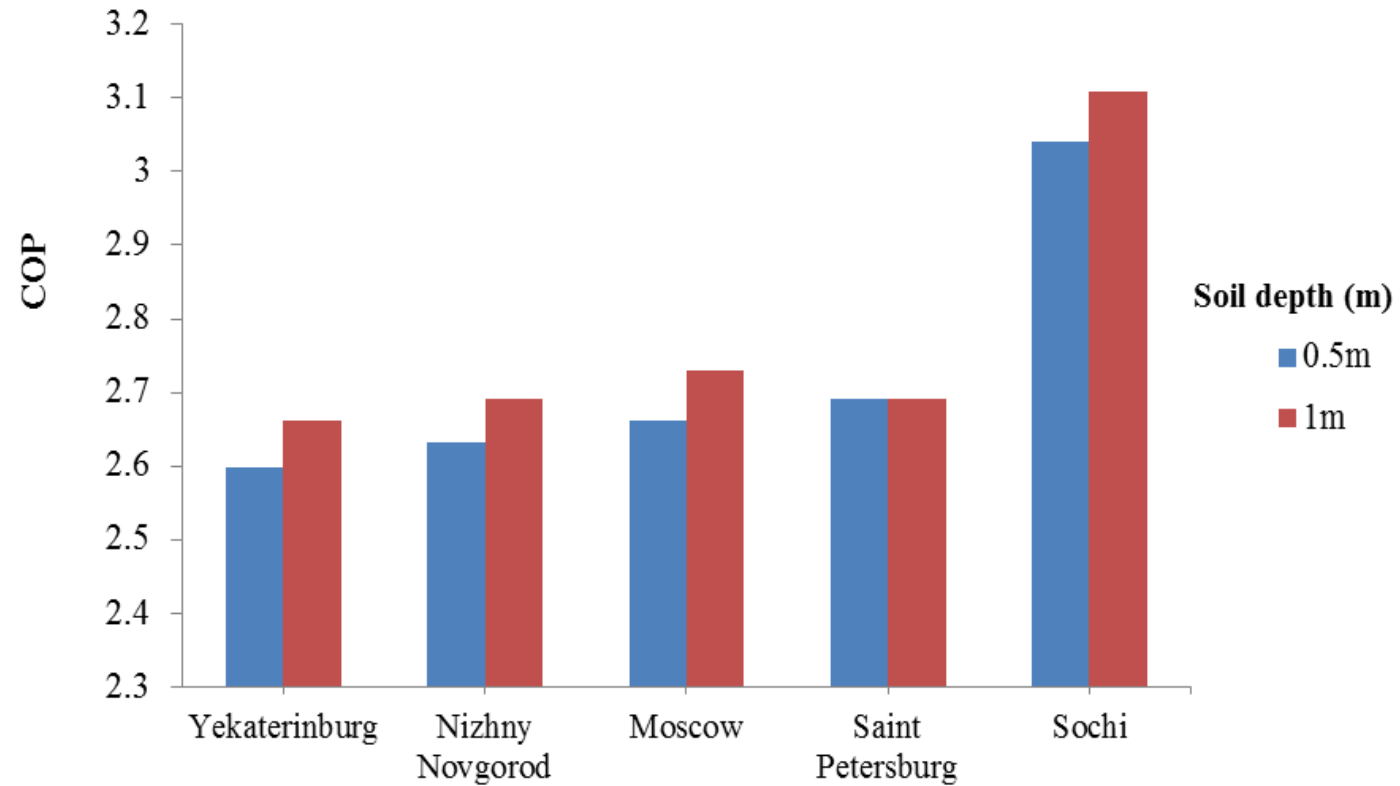
Validation

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Comparison of optimization results for COP



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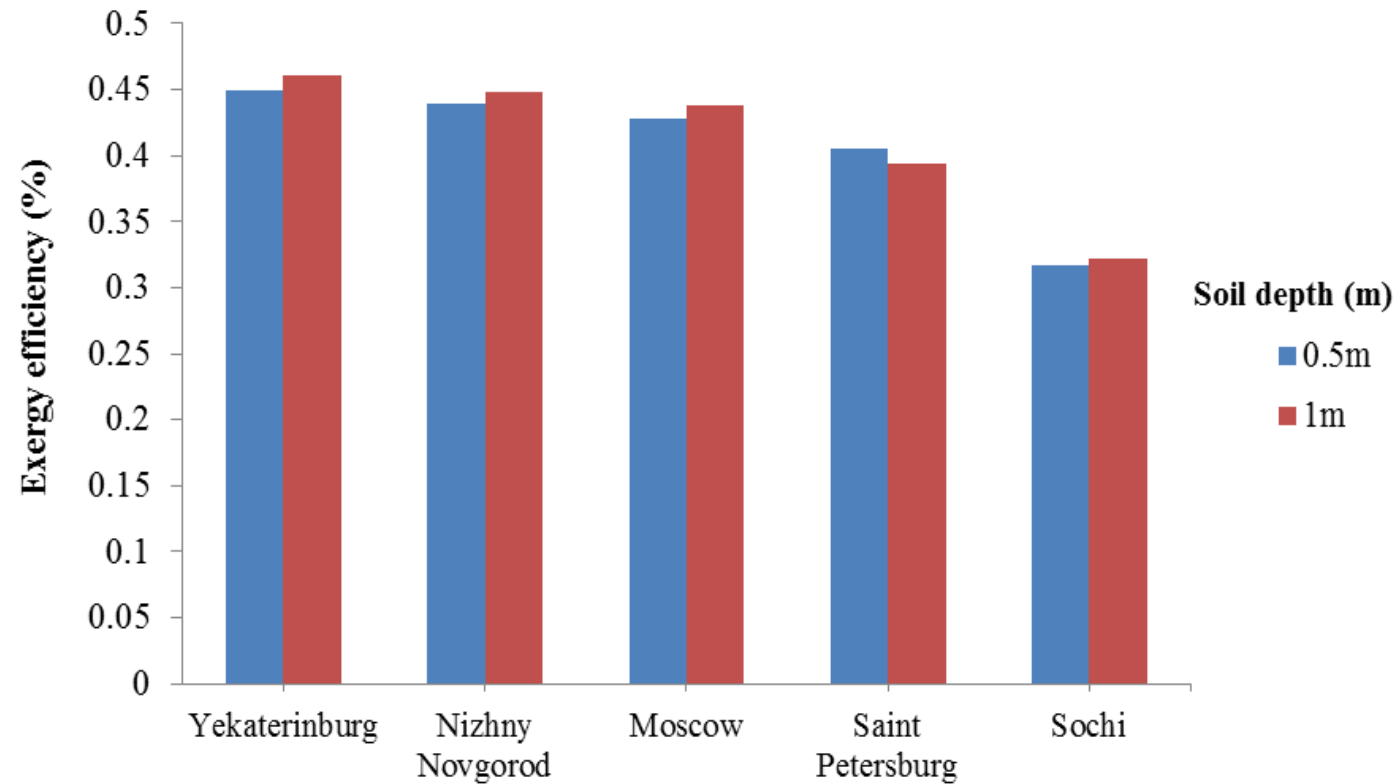
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Comparison of optimization results for exergy efficiency



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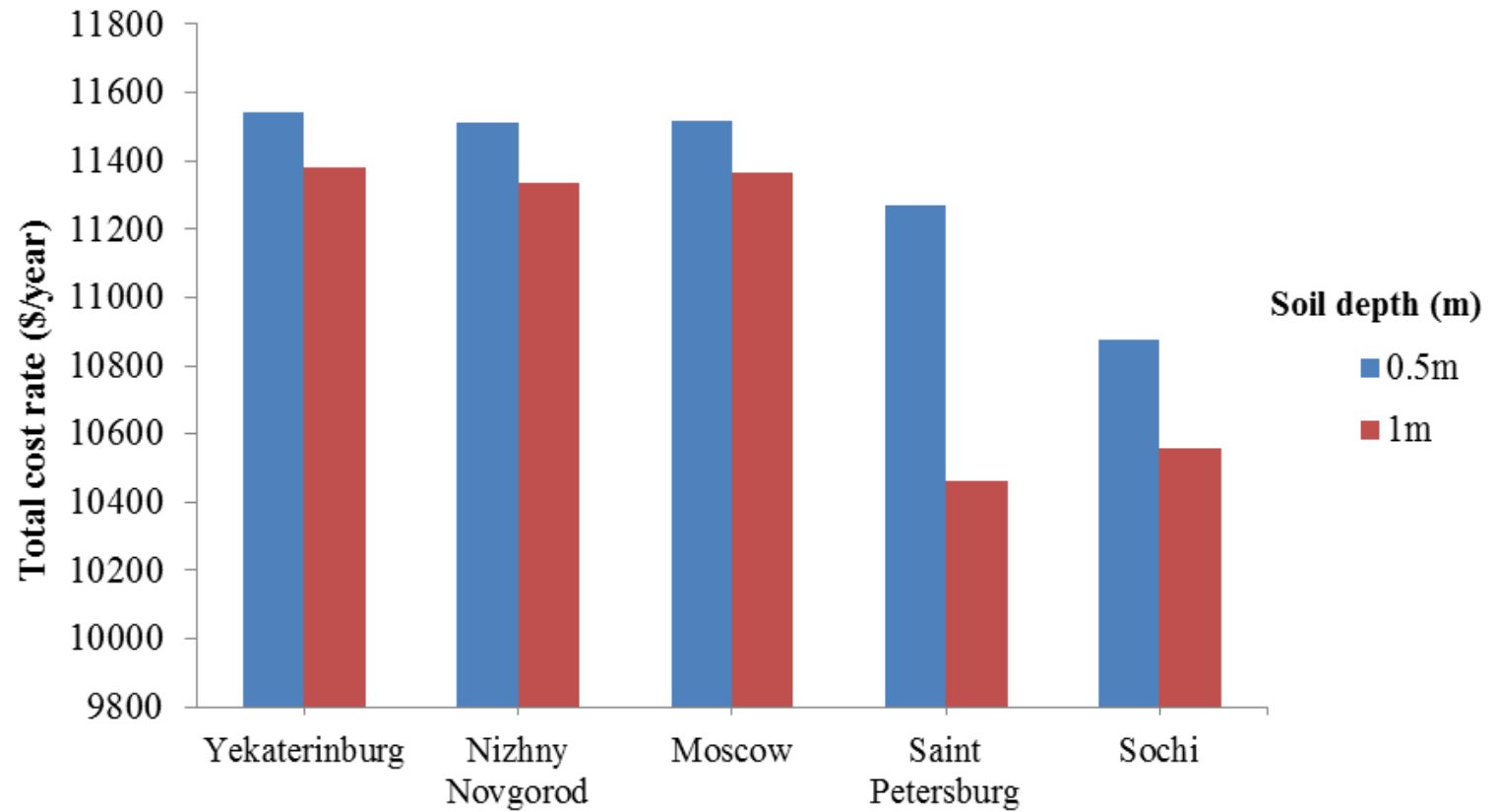
Validation

Optimization

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Comparison of optimization results for total cost rate



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- In optimal point, maximum COP, maximum exergy efficiency and minimum total cost rate are considered to calculate optimal value of evaporator temperature and condensation temperature of cascade heat exchanger
- Increasing evaporator temperature and condensation temperature of cascade heat exchanger leads to increase COP and exergy efficiency and decrease the total cost rate.
- Increasing soil depth leads to increase evaporator temperature and total cost rate due to the increasing cost drilling for higher depth.
- Maximum COP among the 5 cities in Russia is equal to 3.11 for Sochi while maximum exergy efficiency is equal to 0.46 for Yekaterinburg.
- The most cost-effective total cost rate is obtained for Saint Petersburg which is 10462 (\$/year).



Thank you