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III INTERNATIONAL SCIENTIFIC CONFERENCE “SUSTAINABLE AND EFFICIENT USE OF  
ENERGY, WATER AND NATURAL RESOURCES” - SEWAN-2021 ”

## APPLICATION OF MULTIVARIATE ANALYSIS IN TECHNICAL SYSTEMS

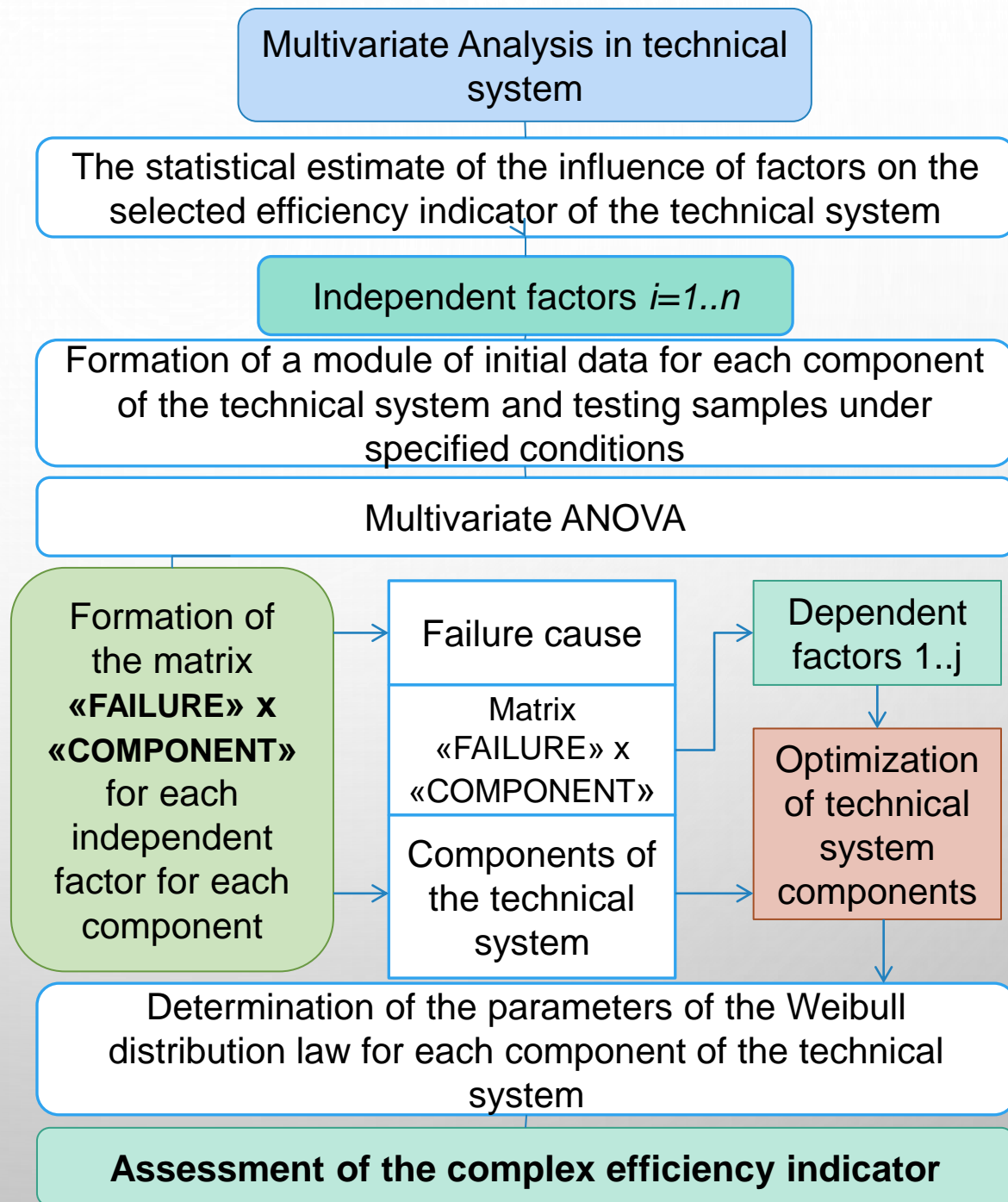
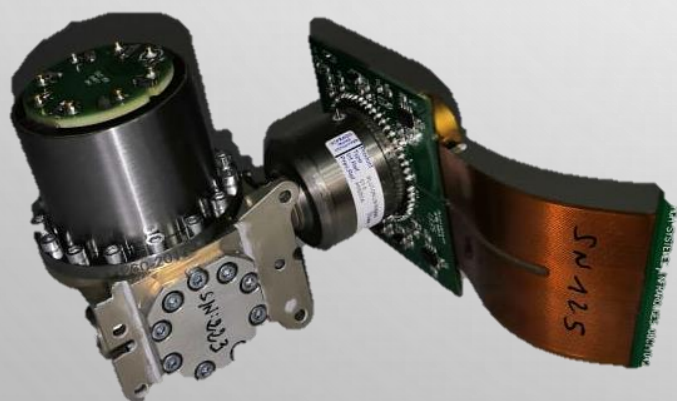
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## ИСПОЛЬЗОВАНИЕ МНОГОФАКТОРНОГО АНАЛИЗА В ТЕХНИЧЕСКИХ СИСТЕМАХ

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# THE STRUCTURE OF MULTIVARIATE ANALYSIS FOR ASSESSING OF THE EFFICIENCY INDICATOR





## Special application of microcryocoolers:

- ✓ In cryostatting systems for PC – thermal imaging equipment in weapon sights and night vision devices;
- ✓ In thermal imaging channels of air defense systems (warning systems) and other guidance systems and fire control systems of armored combat vehicles (AFV);
- ✓ In aircraft protection systems;
- ✓ In coast guard systems;
- ✓ As part of onboard cooling systems for infrared surveillance spacecraft;
- ✓ In Mega pixel format FPAs systems of matrix photodetectors;
- ✓ In cryostatting systems for photosensitive elements of infrared receivers;
- ✓ In security systems high-density urban areas;
- ✓ In security system for airoports, military facilities and research institutions;
- ✓ In UAV control systems;
- ✓ In tracking antenna systems.

## General technical systems:

- ✓ Medical equipment;
- ✓ Telecommunication equipment;
- ✓ Superconducting and scientific products;
- ✓ Non-destructive testing systems;
- ✓ Gas leak detection systems;
- ✓ PC spectrophotometers;





# REVIEW OF METHODS FOR DETERMINING THE OPERATING TIME (MTTF – MEAN TIME TO FAILURE) OF VARIOUS MANUFACTURERS OF MICROCRYOCOOLERS

Methods for predicting the reliability of microcryocooler manufacturers: «Thales Cryogenic» (Sweden, France) and «Ricor» (Israel):

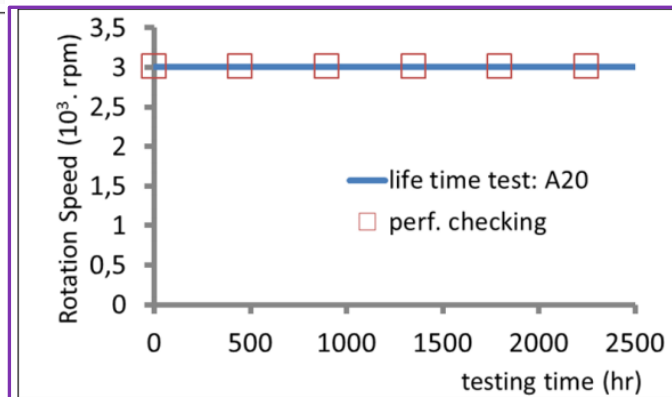
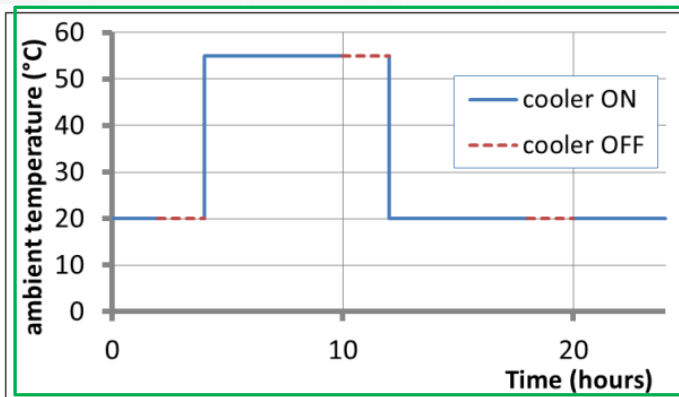


Fig.1 Standard tests of MTTF (at 20 °C)

Fig.2 Accelerated tests A20 n=3000 rpm

$$f(x, \beta, \eta) = \frac{\beta}{\eta} \left(\frac{x}{\eta}\right)^{\beta-1} e^{-(x/\eta)^\beta}$$

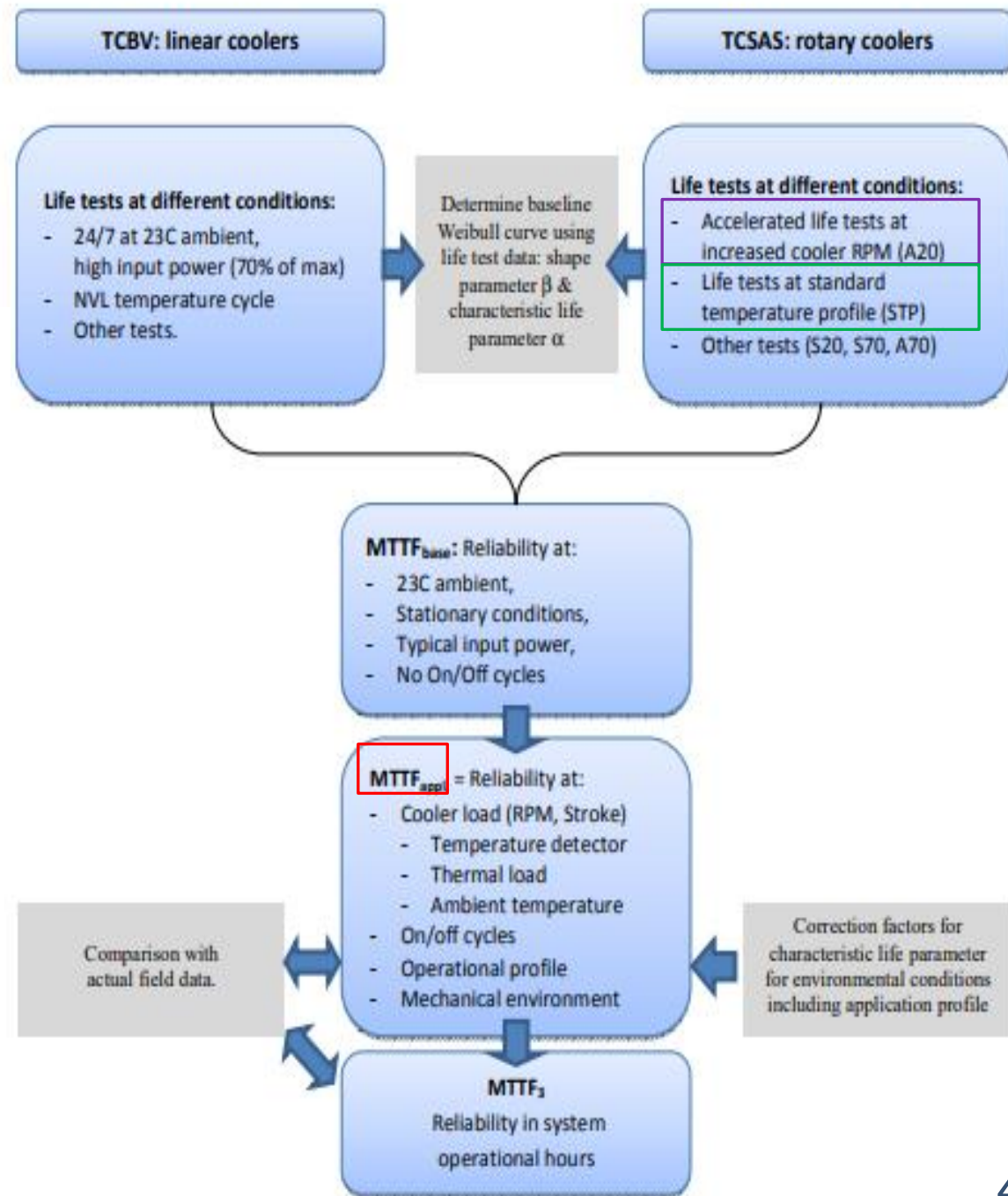
$\beta$  – shape factor;  
 $\eta$  – scale factor.

$$MTTF = \sum_{i=1}^n \frac{t_i}{m}$$

$t_i$  – time to failure;  
 $n$  – number of tested machines;  
 $m$  – number of failures.

Determination of the MTTF value taking into account the field of application:

$$MTTF_{\alpha n} = \left(\frac{RPM_{A20}}{RPM_{T\alpha n}}\right)^{1,5} MTTF_{A20 \text{ test Weibull}} C_{1\alpha n}$$



# REVIEW OF METHODS FOR DETERMINING THE OPERATING TIME (MTTF – MEAN TIME TO FAILURE) OF VARIOUS MANUFACTURERS OF MICROCRYOCOOLERS

## «BAE System» (Great Britain)

Prediction of the MTTF (reliability) is estimated in Watt-hours:

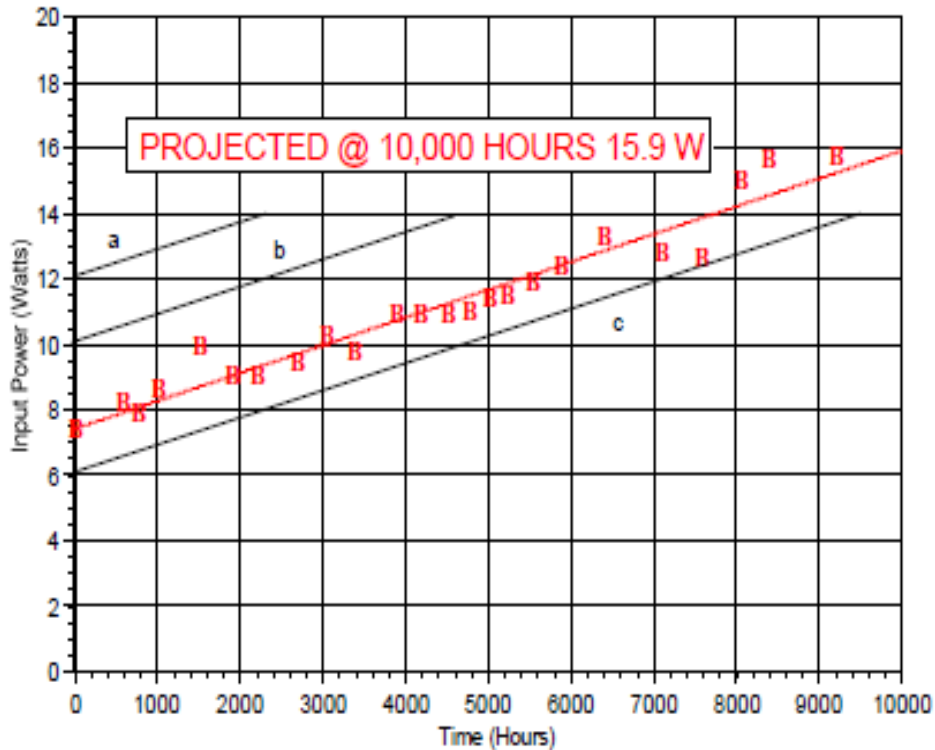


Fig.3 Power consumption: a -12W, b-10W, c – 8 W

### Advantage of the «BAE System» method:

Prediction the mean time to failure under different operating conditions of the MTTF of the same series.

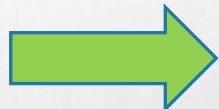
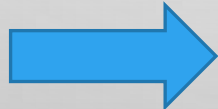
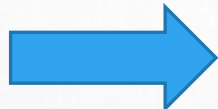
### Disadvantages of the presented methods:

- a large number of tests;
- prediction of the operating time of the microcryocooler assembly and the impossibility of separately assessing the operating time of units and parts included in the assembly;
- applicability of the method only to manufactured equipment;
- predicting reliability with a probability of 63,2%!!!

# IDENTIFICATION INDEPENDENT & DEPENDENT VARIABLES

## ➤ INDEPENDENT VARIABLES

- ❑ **External factors:**
  - Ambient temperature (-60...+60°C);
  - Ambient pressure (1...10 bar).
- ❑ **Design solutions:**
  - Design and porous of the regenerator;
  - Change working substance;
  - The size of clearance between the piston-cylinder (2...14µm).
- ❑ **Technical features:**
  - Filling pressure (2,5..4,0 MPa);
  - Rotation speed (1600...3000 rpm).

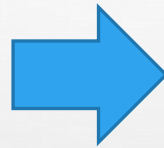


## ➤ DEPENDENT VARIABLE

- **Cooling capacity  $\leq 500\text{mW}$**
- **Power Consumption  $\leq 20\text{W}$**
- **COP**
- **Cooling temperature  $\leq 77\text{K}$**
- **MTTF (Mean Time To Failure)**

**Table №1. The Input data for the analysis of the influence on the dependent factor of the main independent factors A, B, C, D**

Factor - A	Factor - B	Factor - C			
		Value 1		Value ... n	
		Independent factor- D		Independent factor- D	
		Value 1	Value k	Value 1	Value k
Value 1	Value 1	R1 <sub>11</sub>	R7 <sub>k1</sub>	R13 <sub>11</sub>	R19 <sub>k1</sub>
	Value j	R2 <sub>1j</sub>	R8 <sub>kj</sub>	R14 <sub>1j</sub>	R20 <sub>kj</sub>
...	Value 1	R3 <sub>11</sub>	R9 <sub>k1</sub>	R15 <sub>11</sub>	R21 <sub>k1</sub>
	Value j	R4 <sub>1j</sub>	R10 <sub>kj</sub>	R16 <sub>1j</sub>	R22 <sub>kj</sub>
Value i	Value 1	R5 <sub>11</sub>	R11 <sub>k1</sub>	R17 <sub>11</sub>	R23 <sub>k1</sub>
	Value j	R6 <sub>1j</sub>	R12 <sub>kj</sub>	R18 <sub>1j</sub>	R24 <sub>kj</sub>



**Table №2. Experimental operating time values of a microcryocooler  $t$  (hour), grouped for multivariate analysis of variance**

T ambient, °C	Filling pressure, bar	The size of the clearance between the piston and the cylinder, $\mu\text{m}$			
		$\delta=6$		$\delta=10$	
		Rotor speed n, rpm		Rotor speed n, rpm	
		n=1600	n=3000	n=1600	n=3000
Plus 60	32	$t_{1k}$ $k=1 \dots m$	$t_{10k}$ $k=1 \dots m$	$t_{19k}$ $k=1 \dots m$	$t_{28k}$ $k=1 \dots m$
	35	$t_{2k}$ $k=1 \dots m$	$t_{11k}$ $k=1 \dots m$	$t_{20k}$ $k=1 \dots m$	$t_{29k}$ $k=1 \dots m$
	40	$t_{3k}$ $k=1 \dots m$	$t_{12k}$ $k=1 \dots m$	$t_{21k}$ $k=1 \dots m$	$t_{30k}$ $k=1 \dots m$
Plus 20	32	$t_{4k}$ $k=1 \dots m$	$t_{13k}$ $k=1 \dots m$	$t_{22k}$ $k=1 \dots m$	$t_{31k}$ $k=1 \dots m$
	35	$t_{5k}$ $k=1 \dots m$	$t_{14k}$ $k=1 \dots m$	$t_{23k}$ $k=1 \dots m$	$t_{32k}$ $k=1 \dots m$
	40	$t_{6k}$ $k=1 \dots m$	$t_{15k}$ $k=1 \dots m$	$t_{24k}$ $k=1 \dots m$	$t_{33k}$ $k=1 \dots m$
Minus 60	32	$t_{7k}$ $k=1 \dots m$	$t_{16k}$ $k=1 \dots m$	$t_{25k}$ $k=1 \dots m$	$t_{34k}$ $k=1 \dots m$
	35	$t_{8k}$ $k=1 \dots m$	$t_{17k}$ $k=1 \dots m$	$t_{26k}$ $k=1 \dots m$	$t_{35k}$ $k=1 \dots m$
	40	$t_{9k}$ $k=1 \dots m$	$t_{18k}$ $k=1 \dots m$	$t_{27k}$ $k=1 \dots m$	$t_{36k}$ $k=1 \dots m$



$t_1 \dots t_{36k}$  – the values of the dependent factor (operating time of the tested samples of the microcryocooler)



# The statistical estimate of the degree of influence of independent factors on the selected microcryocooler efficiency indicator (MTTF - mean time to first failure) in STATGRAPHICS©Centurion XVI

## The results of calculating P-value when assessing the influence of independent factors:

- filling pressure (3,2..3,5..4,0МПа),
- ambient temperature (+65 °С, +20 °С, -60 °С),
- clearance between the piston and the cylinder  $\delta$  (6 и 10 $\mu$ m)
- rotor speed (1600 rpm & 3000 rpm)

Multifactor ANOVA - Operation time to failure

Analysis of Variance for Operation time to failure - Type III Sums of Squares

Source	Sum of Squares	Df	Mean Square	F-Ratio	P-Value
<b>MAIN EFFECTS</b>					
A:Filling pressure	171349,	2	85674,3	416,20	0,0000
B:Ambient temperature	528345,	2	264173,	1283,35	0,0000
C:Rotation speed	246636,	1	246636,	1198,15	0,0000
D:Clearance	34,7222	1	34,7222	0,17	0,6816
<b>INTERACTIONS</b>					
AB	83224,1	4	20806,0	101,08	0,0000
AC	999,299	2	499,649	2,43	0,0902
AD	5,21528	2	2,60764	0,01	0,9874
BC	830,84	2	415,42	2,02	0,1349
BD	242,528	2	121,264	0,59	0,5555
CD	129,337	1	129,337	0,63	0,4287
RESIDUAL	55166,9	268	205,847		
TOTAL (CORRECTED)	1,08696E6	287			

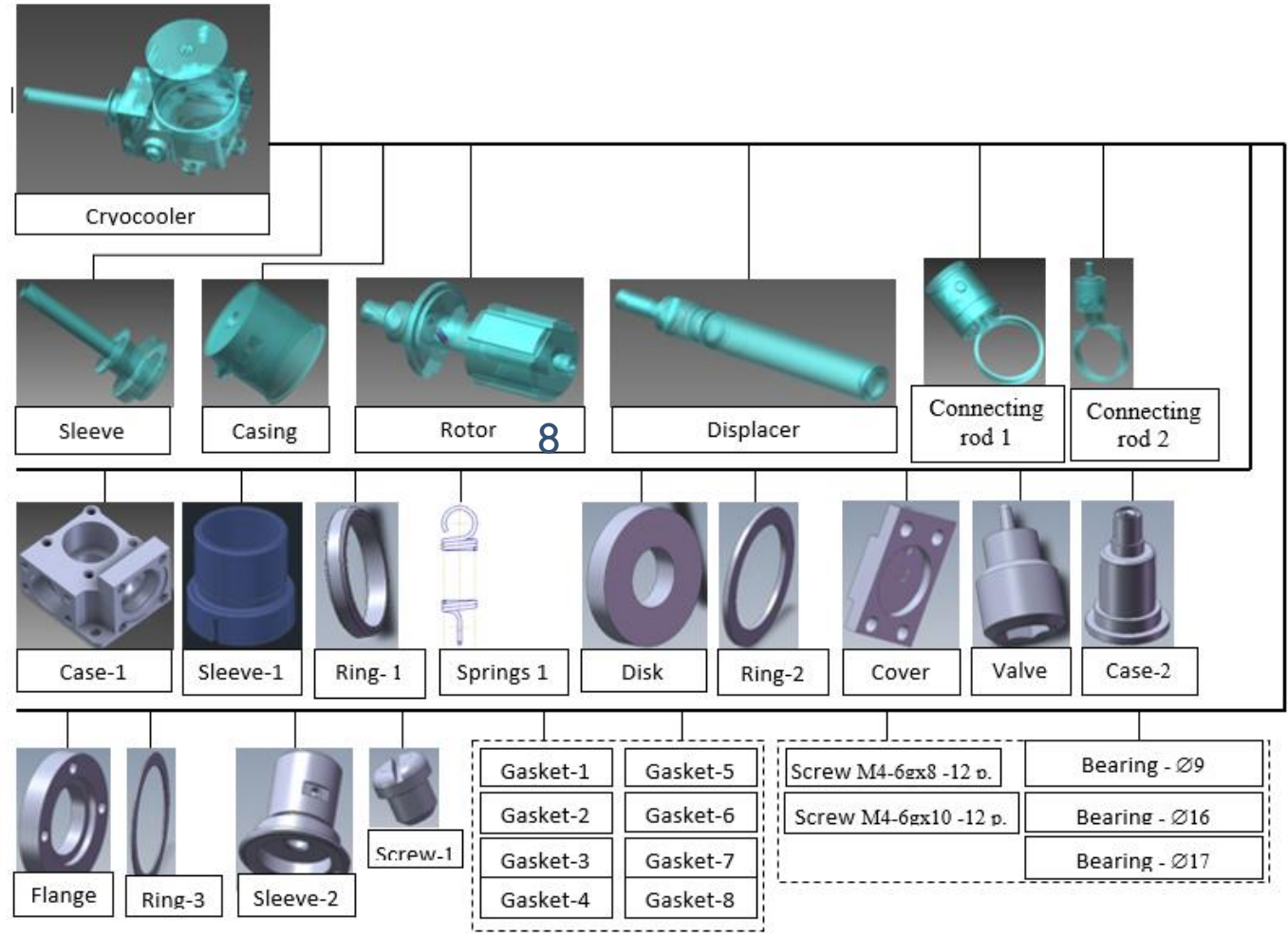


**P ≤ 0.05 – ambient temperature, filling pressure, rotor speed have a decisive influence on the resource of the microcryocooler** !

**P ≥ 0.05 – the size of the clearance does not have a significant effect on the resource of the microcryocooler in the range from 6 to 10 μm**



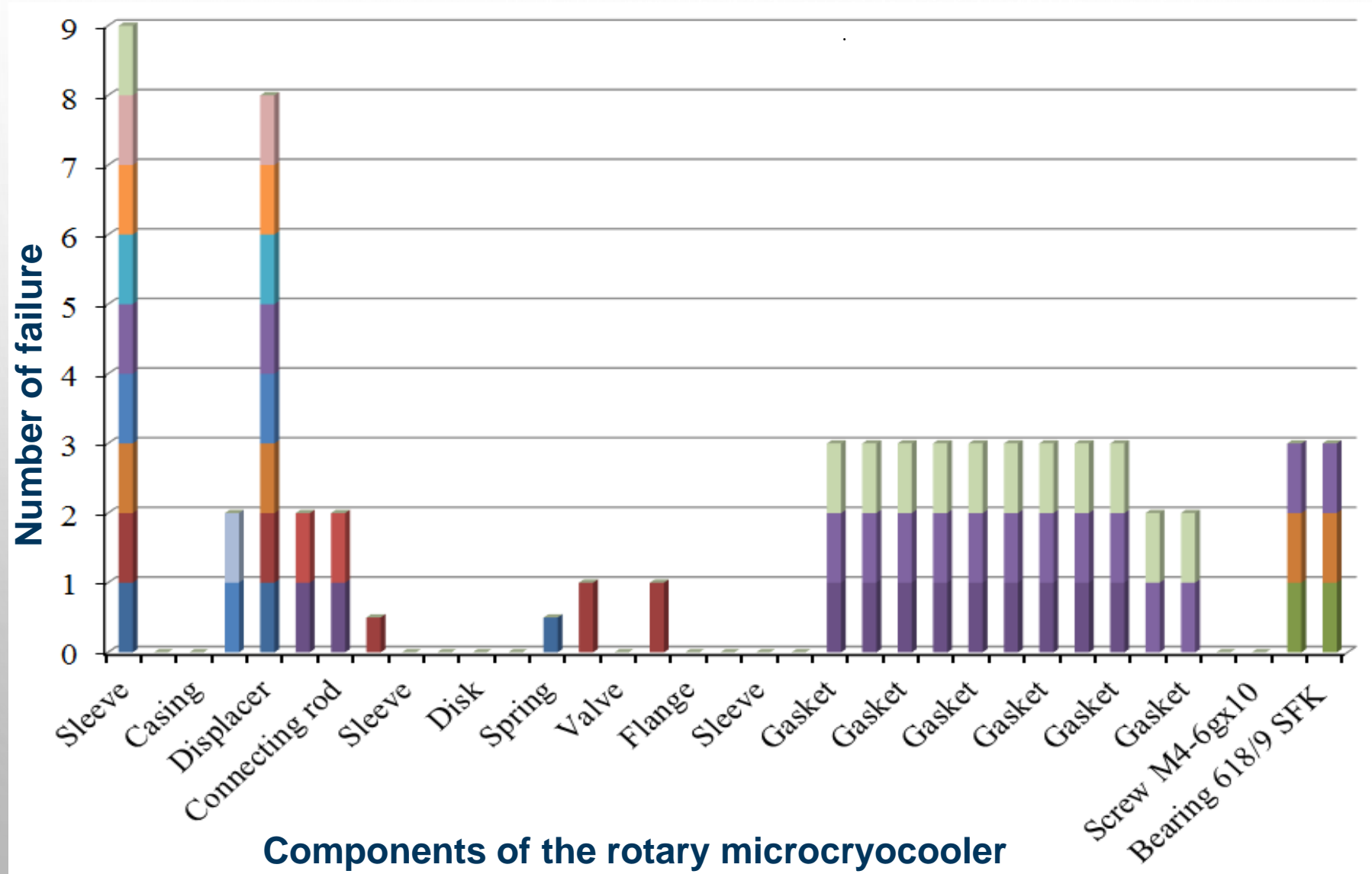
# Sample of filling the Matrix «FAILURE» x «COMPONENTS» for rotary-type of the microcryocooler



COMPONENTS -Vector «C»  
FAILURE – Vector «F»

Component «C»	COMPONENT	Destruction	Corrosion	Fatigue	Crack	Jamming and scuffs	Human factor	Disturbance due to stress	Wear	Critical growth in power consumption	Critical increase in the hydro-resistance of the regenerator	Vibration critical	Cryostation temperature rise	Leakage of working substance
		F1	F2	F3	F4	F5	F6	F7	F8	F9	F10	F11	F12	F13
C1	Sleeve (Assembly)	0	0	0	0	1	1	0	1	1	1	0	0	1
C2	Stator (A)	0	0	0	0	0	0	0	0	0	0	0	0	0
C3	Casing (A)	0	0	0	0	0	0	0	0	0	0	0	0	0
C4	Rotor (A)	0	1	0	0	1	1	0	1	0	0	1	0	0
C5	Displacer (A)	0	1	0	0	0	0	0	0	0	0	0	1	0
C6	Connected rod 1	0	0	0	1	0	0	1	0	0	0	0	0	0
C7	Connected rod 1	0	0	0	1	0	0	1	0	0	0	0	0	0
C8	Case-1 (Detail)	0	1	0	0	0	0	0	0	0	0	0	0	0
C9	Sleeve-1 (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C10	Ring-1 (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C11	Disk (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C12	Ring-2 (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C13	Springs-1 (D)	1	0	0	0	0	0	0	0	0	0	0	0	0
C14	Cover (D)	0	1	0	0	0	0	0	0	0	0	0	0	0
C15	Valve (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C16	Case-2 (D)	0	1	0	0	0	0	0	0	0	0	0	0	0
C17	Flange (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C18	Ring-3 (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C19	Sleeve-2 (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C20	Screw-1 (D)	0	0	0	0	0	0	0	0	0	0	0	0	0
C21	Gasket-1(D)	0	0	0	1	0	0	0	1	0	0	0	0	1
C22	Gasket-2(D)	0	0	0	1	0	0	0	1	0	0	0	0	1
C23	Gasket-3(D)	0	0	0	1	0	0	0	1	0	0	0	0	1
C24	Gasket-4(D)	0	0	0	1	0	0	0	1	0	0	0	0	1
C25	Gasket-5(D)	0	0	0	1	0	0	0	1	0	0	0	0	1

# The overall FAILURE DIAGRAM for each component in the microcryocooler





## 1. Multivariate analysis in the technical systems allows:

- To identify the factors that have the greatest impact on the efficiency indicator and on a frequent cause of failure;
- to determinate the depth and sequence of improving units and parts included in the assembly;
- to design equipment for the given operating conditions at the design stage;
- To predict of resource.

2. Matrix «FAILURE» & «COMPONENT» is informative because it shows the most loaded components when there is **no test data**.

3. The combination of independent factors that have the greatest impact on the resource is basis for further optimization of units and parts of the technical system for the specified operating conditions.



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**THANK YOU**  
**QUESTION?**

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